

Name: \_\_\_\_\_  
Student ID: \_\_\_\_\_

## Quiz 8

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

**Question 1.** (5 marks) §6.6 #21 Determine whether each integral is convergent or divergent. Evaluate those that are convergent.

$$\int_{-\infty}^{\infty} \frac{x^2}{9+x^6} dx$$

**Question 2.** (5 marks) §7.1 #8 Sketch the region enclosed by the given curves. Then find the area of the region.

$$y = 1 + \sqrt{x}, \quad y = 1 + \frac{1}{3}x$$

**Question 3.** (5 marks) If  $f(0) = g(0) = 0$  and  $f''$  and  $g''$  are continuous, show that

$$\int_0^a f(x)g''(x) \, dx = f(a)g'(a) - f'(a)g(a) + \int_0^a f''(x)g(x) \, dx$$