Dawson	College:	Introduction (	to Annlied	Mathematics:	201-	912-DW	Fall 2015
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Name:	
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## Test 2

This test is graded out of 50 marks. No books, notes, graphing calculators or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page. This test consists of 9 questions and one bonus question. The maximum possible grade is 50/50. Please ensure that you have a complete test. This test must be returned intact.

Question 1. Newton's Law of Cooling (Warming)<sup>1</sup>: The temperature T of an object at time t is given by the formula

$$T(t) = T_a + (T_0 - T_a)e^{-kt}$$

where  $T(0) = T_0$  is the initial temperature of the object,  $T_a$  is the ambient temperature and k > 0 is the constant of proportionality.

A 50°C object is cooked in a 350°C oven. After 3 hours the temperature of the object is 90°C.

- a. (2 marks) Assuming the temperature of the object follows Newton's Law of Warming, find a formula for the temperature of the object *T* as a function of its time in the oven, *t*, in hours.
- b. (2 marks) The object is done cooking when the internal temperature reaches 225°C. After how many hours will the object be cooked?

**Question 2.** $^2$  (4 marks) Solve for x.

$$\log_3(x-4) + \log_3(x+4) = 2$$

<sup>&</sup>lt;sup>1</sup>from Precalculus, version 3, Carl Stitz and Jeff Zeage, 2011

<sup>&</sup>lt;sup>2</sup>from Precalculus, version 3, Carl Stitz and Jeff Zeage, 2011



**Question 4.** (6 marks) How much of each of the following mixtures must be used in order to make a 20m<sup>3</sup> mixture which has 15% sand, 35% aggregate and 50% cement.

Mix A: 10% sand, 30% aggregate and 60% cement Mix B: 20% sand, 10% aggregate and 70% cement Mix C: 10% sand, 80% aggregate and 10% cement

**Question 5.** (4 marks) Solve the following linear system using Cramer's rule.

$$\begin{array}{rcrr} x_1 & - & 2x_2 = & 5 \\ 3x_1 & - & 4x_2 = & -6 \end{array}$$

**Question 6.** (4 marks) Graph the function  $f(x) = 4 - 2^{-x}$ 

## Question 7.

a. (4 marks) Find the center and the radius of the circle. hint: complete the square for the variable y

$$x^2 + y^2 - 8y + 12 = 0$$

- b. (4 marks) Find the standard equation of the ellipse  $4x^2 + 9y^2 36 = 0$ . Identify the center and vertices of the ellipse.
- c. (4 marks) Solve the non-linear system

$$x^{2} + y^{2} - 8y + 12 = 0$$
$$4x^{2} + 9y^{2} - 36 = 0$$

d. (3 marks) Sketch both curves from c. on the same graph.

Question 8. Expand the given logarithms and simplify as much as possible:

a. (2 marks)

$$\log_3\left(\frac{81\sqrt{x}\ y^5}{z}\right)$$

b. (2 marks)

$$\ln\left(x^2(x+3)\right)$$

**Question 9.** Use the properties of logarithms to write each expression as a single logarithm:

a. (2 marks)

$$3\ln x + \frac{1}{3}\ln y - 2\ln z$$

b. (2 marks)

$$\log_5 x - \log_{25} x$$

**Bonus Question.** (3 marks) Find the radius of the circle with center (4, -3) and tangent to the line y = 2x - 1