

Question 1. (10 marks) Use the simplex method to solve the linear programming problem: Maximize the objective function: $x = 5x_1 + 2x_2 + 8x_3$ subject to

$$\begin{cases} 2x_1 - 4x_2 + x_3 \leq 42 \\ 2x_1 + 3x_2 - x_3 \leq 42 \\ 6x_1 - x_2 + 3x_3 \leq 42 \end{cases}.$$

Explicitly write the final value of the objective function, variables and slack variables.

Bonus Question. (2 marks) The barber is the "one who shaves all those, and those only, who do not shave themselves". The question is, does the barber shave himself?