

Quiz 5

This quiz is graded out of 10 marks. No books, calculators, notes or cell phones are allowed. You must show all your work, the correct answer is worth 1 mark the remaining marks are given for the work. If you need more space for your answer use the back of the page.

Question 1. §7.1#35 (6 marks)

Find the area bounded by the two curve $y = x^2 - 4x + 3$ and $y = 3 + 4x - x^2$ and give a graph of both curves.

First we find where both curves intersect: $x^2 - 4x + 3 = 3 + 4x - x^2$
 $2x^2 - 8x = 0 \Rightarrow x = 0, 4$ ← the curves intersect at

Do the curves cross the x-axis: yes

The vertex of the two quadratic

$$y = x^2 - 4x + 3 = x^2 - 4x + 4 - 4 + 3 = (x - 2)^2 - 1 \quad \therefore \text{vertex at } (2, -1)$$

$$y = 3 + 4x - x^2 = -(x^2 - 4x - 3) = -(x^2 - 4x + 4 - 4 - 3) = -(x - 2)^2 + 7 \quad \therefore \text{vertex at } (2, 7)$$

$$\text{Area} = \int_0^4 (3 + 4x - x^2) - (x^2 - 4x + 3) dx = \int_0^4 8x - 2x^2 dx$$

$$= 4x^2 - \frac{2}{3}x^3 \Big|_0^4$$

Question 2. §8.1#11 (4 marks)

Integrate the following indefinite integral using integration by parts:

$$\int x e^{-2x} dx \quad \int u dv = uv - \int v du$$

Let $u = x \Rightarrow du = dx$

$$v = -\frac{e^{-2x}}{2} \leftarrow dv = e^{-2x} dx$$

$$= -\frac{x e^{-2x}}{2} - \int -\frac{e^{-2x}}{2} dx$$

$$= -\frac{x e^{-2x}}{2} - \frac{e^{-2x}}{4} + C$$

Bonus. (1 mark)

List the three trigonometric identities given last class.

$$\sin^2 x + \cos^2 x = 1$$

$$\cot^2 x = \csc^2 x - 1$$

$$\tan^2 x = \sec^2 x - 1$$

